Message Authentication Using Proxy Vehicles in Vehicular Ad Hoc Networks

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Abstract—Normally, authentication in vehicular ad-hoc networks (VANETs) uses Public Key Infrastructure (PKI) to verify the integrity of messages and the identity of message senders. The issues considered in the authentication schemes include the level of security and computational efficiency in verification processes. Most existing schemes focus mainly on assuring the security and privacy of VANET information. However, these schemes may not work well in VANET scenarios. For instance, it is difficult for a RoadSide Unit (RSU) to verify each vehicle’s signature sequentially when a large number of vehicles emerge in the coverage areas of an RSU. To reduce the computational overhead of RSUs, we propose a Proxy Based Authentication Scheme (PBAS) using distributed computing. In PBAS, proxy vehicles are used to authenticate multiple messages with a verification function at the same time. In addition, RSU is able to independently verify the outputs from the verification function of the proxy vehicles. We also design an expedite key negotiation scheme for transmitting sensitive messages. It is shown from the analysis and simulations that an RSU can verify 26500 signatures per second simultaneously with the help of the proxy vehicles. The time needed to verify 3000 signatures in PBAS can be reduced by 88% if compared to existing batch-based authentication schemes.

Index Terms—Proxy vehicle; Proxy based authentication; Key negotiation; Privacy preservation; Vehicular ad-hoc network.

I. INTRODUCTION

VANETs have attracted a lot of attention due to its potential to offer better driving experience and road safety, as well as many other value-added services [1] [2]. Security issue [3] [4] is critical in VANETs because many different forms of attacks [3] against VANETs may emerge due to the use of wireless devices in VANET communications. Such security attacks may lead to bad user experience (thus causing the loss of revenue for those value-added service providers) or create even more catastrophic consequences such as the loss of lives due to the traffic accidents due to the failure of VANET communications.

Some sophisticated security schemes have been proposed in the literature as an effort to ensure that all information exchanged in VANETs is authenticated and thus can be fully trusted. In particular, Raya et al. presented a Public-Key Infrastructure (PKI) based scheme for vehicular signature applications [1], where an RSU verifies received messages one after another. Because vehicles normally forward messages on the fly at any time, it may not be able to be predicted and known by RSU. Also, those PKI-based schemes [1] [5] [6] are time-consuming processes and may fail to satisfy the computational efficiency requirement under dynamic traffic patterns, where the computational complexity and transmission overhead of RSUs increase linearly with the number of vehicles that need to be authenticated.

Zhang et al. in their work published in [7] introduced an efficient batch signature verification scheme for the communications between vehicles and RSUs, in which an RSU can verify multiple received signatures at the same time, such that the total verification time required can be significantly reduced. In their proposed scheme, an RSU can simultaneously verify approximately 1600 messages per second, which is not bad but still not fast enough to meet the requirement of VANET authentication speed. According to the Dedicated Short Range Communications (DSRC) protocol [8] [9], each vehicle broadcasts a traffic safety message every 100~300 ms. This implies that an RSU must verify around 2500~5000 messages per second when there are 500 vehicles within the coverage of an RSU, which is indeed a great challenge for any current batch-based digital signature scheme reported in the literature [10] [11] [12] [13].

In this paper, our goal is to tackle the aforementioned efficiency problem of the existing authentication schemes. In particular, we will propose a Proxy Based Authentication Scheme (PBAS) for this purpose. In this proposed scheme, each proxy vehicle plays an important role, which is adopted to authenticate multiple messages with the help of a verification function at the same time. In this way, the distributed computing can be used to shed the time-consuming centralized computing loads at RSUs. We also design a systematic and independent mechanism for RSUs to verify the output of the verification function from different proxy vehicles, by which an RSU can evaluate the validity levels of different messages in the same way as done in separate verification schemes. In addition, batch key negotiations can also be accomplished in the proposed scheme, in which an RSU can complete the batch process of vehicles’ key negotiations by broadcasting a single
The scheme has the property that enables the verification process to continue even in the event that a small number of proxy vehicles have been compromised in VANETs (see Section V).

The remainders of this paper can be outlined as follows. Section II surveys the related works in the literature. Section III introduces the system and security models, together with the related preliminaries. Section IV is to discuss the issues on proxy based batch authentication scheme (PBAS). Section V is to conduct security performance analysis. Section VI is dedicated for complexity evaluation and simulations for PBAS and the other existing authentication schemes, followed by the conclusions made in Section VII.

II. RELATED WORKS

In the current IEEE 1609.2 standard [9], vehicular communication messages should be authenticated using the Elliptic Curve Digital Signature Algorithm (ECDSA) [14]. Each message also includes a certificate. As shown by the analytical study conducted in [15], a major challenge that remains to be tackled is to find a way to reduce the resource consumptions in computation and transmission. In the text followed, we will discuss about the two authentication schemes that have been proposed in the literature.

A. Conventional Authentication

Let us start with the discussions about the prior works on the ECDSA-based schemes, and will take this scheme as an example to explain the important relationship between the integrity of messages and the validity of sender’s identities. Studer et al., pointed out in their work [5] that a VANET user needs to verify the validity of the identity of a message sender before verifying the integrity of the messages it sends out. If the system designers focus only on the mechanisms to verify messages and ignore the importance associated with the verification of valid entities, a malicious participant could exploit many forged identities to disable VANET communications. Therefore, they particularly proposed TESLA++ [5] as a modified version of TESLA [16], which combines the advantages of ECDSA signatures and TESLA. Compared with TESLA, TESLA++ takes the advantage of relatively shorter Hash Message Authentication Code (HMAC) to verify the integrity of messages, which helps to cut down the transmission overhead of RSUs. If compared with TESLA, TESLA++ signs on each message before its transmission, which is to perform the identity authentication that provides on-repudiation of attribution in multi-hop communications. Any receiver can use the signer’s public key to verify the identity of the message. To verify the messages from the vehicles outside the coverage of an RSU, the authors in [6] suggested that the neighboring vehicles could work cooperatively to probabilistically verify only a small percentage of these message signatures.

B. Batch Authentication

On the other hand, batch verification offers an efficient way for verifying signatures in VANETs. Zhang et al., in [7] introduced an Identity-based Batch signature Verification (IBV) scheme for vehicular-to-infrastructure (V2I) communications, which works based on identity-based encryption algorithms [17][18] proposed by Boneh et al.. In the IBV scheme, an RSU can also verify multiple received signatures at the same time such that the computation time can be significantly reduced. Meanwhile, the certificates are not needed in the verification processes, and thus the transmission overhead can be reduced substantially. The IBV scheme can achieve conditional privacy preservation using pseudo identities, and a Trust Authority (TA) is capable of tracing a vehicle’s real identity from its pseudo identity. In [19], Zhang et al., made their effort to enhance the IBV scheme via adopting a group testing technique. The objective of the group testing is to find invalid signatures with a minimal batch verification workload. In [10], Huang et al., proposed an Anonymous Batch Authenticated and Key Agreement (ABAKA) scheme for different value-added services, which can authenticate multiple messages sent from different vehicles and establish different session keys for different vehicles at the same time. The security of the ABAKA scheme is ensured based also on ECDSA. Compared with the basic ECDSA scheme, relatively short signatures are adopted by the ABAKA scheme to reduce the computation and transmission overheads of RSUs. In [20], Chin et al., introduced a Secure and Privacy Enhancing Communications Scheme (SPECS), where any vehicle can form a group with the other vehicles after batch authenticating and can communicate with one another securely without RSUs. However, in [11], Shi-Jinn Horng et al., found out that SPECS is vulnerable to impersonation attacks, and a malicious vehicle can act as an arbitrary vehicle to broadcast fake messages or even counterfeits.
another group member to send fake messages securely among themselves. To deal with this issue, they proposed b-SPECS+ to overcome the weaknesses of SPECS. In [12], Shim et al. proposed a Conditional Privacy preserving Authentication Scheme (CPAS), which is based on Computational Diffie-Hellman (CDH), to bridge the gap between the privacy and non-repudiation requirements. In [13], Li et al. proposed a Rapid Certification Scheme (RCS), in which a VANET leader is responsible to collect the messages of 2 distinct vehicles, and then sends them to RSU. The RSU verifies the batch of messages. The RCS is able to reduce the transmission overhead of RSUs by integrating messages into batches.

C. Certificate Revocation

Based on the discussions made in the previous paragraphs, we understand that the optimized certificate update schemes [24] [22] [23] [24] are promising approaches for efficient authentication in VANETs, but the revocation list will get very long when it is needed to check the time-consuming Certificate Revocation Lists (CRLs). Albert et al. in their work [25] introduced a protocol for V2V communications, called Expedition Message Authentication Protocol (EMAP), which uses keyed Hash Message Authentication Code (HMAC) technique to replace the CRL checking process. It can help to reduce the computation overhead compared to the conventional schemes employing CRL.

D. Tradeoff between Privacy and Non-Repudiation

The authentication schemes require that vehicles in VANETs should publish their certificates or public keys. Even in identity-based signature algorithms, their identifications should be send to destination together with their messages. The privacy issues have attracted much attention because these identity materials are revealed in VANETs. [26] [27] proposed pseudonym changing based authentication schemes to achieve conditional privacy. The term “conditional” here means that, when car attacks occur, the identity information has to be revealed by TA to establish the liability of the attacks. [28] considered that the TA has all cryptographic materials and may abuse its access ability, and thus they proposed a security framework with non-repudiation and conditional privacy, in which TA never knows the user’s private key. The authors in [29] [30] employed a lightweight conditional privacy-preservation scheme with a simple hash-chain technique, which attributes to the reduction of the computational overhead while achieving conditional privacy.

E. Medium Access Control

Future vehicles will the functions of Medium Access Control (MAC) protocols so that the passengers can surf the Internet in the vehicles. [31] provided a secure MAC protocol to access DSRC channels. The secure communication protocol is designed based on authentication scheme to satisfy the requirements of message authentication and integrity, together with non-repudiation and privacy of senders. The protocol takes advantage of time-stamp mechanism to guarantee the freshness of messages.

III. PRELIMINARIES

Before introducing the PBAS scheme proposed in this paper, we would like to offer a brief review on the preliminary knowledge on VANET security in the subsections followed, to facilitate the discussions and performance analysis on the proposed scheme, which will be presented in Section IV.

A. Bilinear Pairing

Let $G_1$ denote an additive group of prime order q, and $G_2$ denote a multiplicative group of the same prime order. Let $P$ be a generator of $G_1$, and $e: G_1 \times G_1 \rightarrow G_2$ be a bilinear mapping with the following properties:

- **Bilinear**: For all $P, R, Q \in G_1$ and $a, b \in Z_q^*$, we have $e(P, P + R) = e(P + R, Q) = e(Q, P) \times e(P, R)$. In particular, $e(aP, bQ) = e(P, Q)^{ab}$.
- **Non-degeneracy**: $e(P, Q) \neq 1$.
- **Computability**: The map $e$ is efficiently computable.

Next, we state the following two underlying problems as the basis for our proposed scheme.

- **CDH** (Computational Diffie-Hellman) problem: For unknown $a, b \in Z_q^*$, and for the given $aP, bP \in G_1$, compute $P^{ab}$.
- **DDH** (Decisional Diffie-Hellman) problem: For unknown $a, b \in Z_q^*$, and for the given $aP, bP, abP \in G_1$, check if $e(aP, bP) \equiv e(abP, P)$.

It is easy to show that the DDH problem is easy to solve, while the CDH problem is extremely hard to solve.

![Fig. 2. A VANET communication system is supported by Dedicated Short Range Communications (DSRC), which offers Vehicle-to-Vehicle (V2V) and Vehicle-to-Infrastructure (V2I) communications. The system should meet the security requirements to ensure that all information data exchanged are authenticated and can be trusted [9].](image)

B. System Model

Fig. 2 introduces a two-layer network model of VANETs with its underlined security layer and communication layer.
The security layer is comprised of a Trust Authority (TA) and tamper proof devices. The TA is trusted by all entities in the system, it is in charge of distributing the secret keys to all entities, and it has an ability for tracing back to the real identity of a vehicle whenever any uncertainty occurs. According to the VANET standard [8] [9], a tamper proof device installed in the OBU of a vehicle is responsible for storing security materials and implementing all crypto operations. On the other hand, the communication layer is comprised of V2I and V2V modules. The V2V communication system provides a 360-degree view of all its peer vehicles within the communication range. The V2I communication and broadcast systems provide traffic and entertainment information for the drivers.

C. Security Model

In [1], Raya et al. defined five basic attacks, including bogus information, cheating with sensor information, ID disclosure of the other vehicles in order to track their locations, Denial of Service (DoS), and masquerading. [32] [33] extended the attack types by introducing replay attack. In this section, we take all those basic attacks into consideration in a VANET of interest, except for “cheating by sensor information” because the research on this particular topic belongs to data-centric trust establishment [34] [35] [36].

The work reported in [37] indicated that security mechanisms of the VANET framework should support different applications and services. Hence, before discussing the security requirements of our scheme, we first consider two application scenarios, namely safety related applications and value-added applications. For the safety related applications, vehicles in danger will send (broadcast or unicast) safety related messages to other entities in VANETs. The entities need to authenticate these messages before utilizing them. In the safety related applications, there are typically no confidentiality requirements on these safety related messages. For the value-added applications, the confidentiality is required. RSUs are registered as the gateways for Internet access, via which the vehicles that request for the services can establish secrecy links with Internet Service Provider (ISP) because most of the services levy charges. Hence, the messages from ISP can satisfy confidentiality through the key generation process between vehicles and RSUs. In summary, the following four security requirements are needed in PBAS:

1) Message integrity and authentication: Messages sent by vehicles can be authenticated to prove that they are indeed sent by authorized entities without being modified or forged. Moreover, RSUs should have an ability to authenticate a large amount of signatures for many vehicles.

2) Identity privacy preserving and traceability: The real identity of a vehicle should be kept anonymous, which is heterogeneous with the other pseudo identities. Any third party should not be able to reveal the real identity of a vehicle by analyzing multiple messages sent from it. However, when the vehicles send malicious information, TA has an ability to reveal the real identities from the pseudo identities of the misbehaved vehicles.

3) Resisting signature replay attacks: Signature replay attacks can be prevented by such a carefully designed scheme. The definition of a signature replay attack can be generalized as an attack that replays the signatures from a different vehicle for the intended or expected RSUs, thereby to fool the RSUs to believe that they have successfully completed the verification of the owner of these signatures.

4) Confidentiality: A server can establish a secure communication link with a requesting vehicle for subsequent communications. For instance, ISP and parking payments systems require that the session key negotiation process generates the keys for confidentiality of their transmitted messages.

IV. PROXY BASED BATCH AUTHENTICATION

In this section, we introduce PBAS, whose algorithm consists of the following four phases, 1) system initialization phase; 2) message signing phase; 3) batch verification by proxy vehicles; and 4) verification by an RSU at the outputs from proxy vehicles. In addition, a key negotiation phase is included if confidentiality is required. The notations used in this section are listed and defined in Table I.

### TABLE I NOTATIONS AND THEIR DEFINITIONS.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Definition</th>
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<tbody>
<tr>
<td>$V_i$</td>
<td>The $i$th vehicle.</td>
</tr>
<tr>
<td>$s_j$</td>
<td>The $j$th private master key of the tamper proof device, where $j \in {1, 2, 3}$.</td>
</tr>
<tr>
<td>$s_r$</td>
<td>The private master key of the RSU.</td>
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<tr>
<td>$PK_k$</td>
<td>The public key of the system, where $k \in {1, 2, r}$.</td>
</tr>
<tr>
<td>$ID_i$</td>
<td>The pseudo identity of the vehicle $V_i$, where $ID_i = (ID_{i1}, ID_{i2})$.</td>
</tr>
<tr>
<td>$SK_i$</td>
<td>The private key of the vehicle $V_i$, where $SK_i = (SK_{i1}, SK_{i2})$.</td>
</tr>
<tr>
<td>$RID_i$</td>
<td>The real identity of the vehicle $V_i$, where $RID_i \in G$.</td>
</tr>
<tr>
<td>$Rs_r$</td>
<td>The real identity of the RSU, where $Rs_r \in Z_q^*$.</td>
</tr>
<tr>
<td>$SK_r$</td>
<td>The private key of the RSU, where $SK_r = (SK_{r1}, SK_{r2})$.</td>
</tr>
<tr>
<td>$T$</td>
<td>The time stamp of messages.</td>
</tr>
<tr>
<td>$M_i$</td>
<td>A message from vehicle $V_i$.</td>
</tr>
<tr>
<td>$h(\cdot)$</td>
<td>A one-way hash function such as SHA-1, SHA-2.</td>
</tr>
<tr>
<td>$H(\cdot)$</td>
<td>A MapToPoint hash function such as $H : {0, 1}^* \rightarrow G$.</td>
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A. System Initialization

The TA (as shown in Fig. 2) initializes the system parameters for each registered VANET member. Each vehicle generates its pseudo identity and the corresponding key. According to the IEEE standard for VANETs [9], each vehicle should be equipped with a tamper proof device, and no adversary can attain any data stored in the tamper-proof device. The system initialization phase can be modeled mathematically as follows.

- **System parameters generation:**
  1. The TA stores $U_V = \{RID_i | 1 \leq i \leq n\}$.
  2. Given the bilinear parameters $(P, q, G_1, G_2, e)$, the TA chooses four random numbers, i.e., $s_1, s_2, s_3, s_r \in Z_q^*$. 

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3) The TA computes $PK_1 = s_1 P$, $PK_2 = s_2 P$, and $SK_2^{\text{t}} = s_3 P$.
4) The tamper-proof device of each vehicle is secretly preloaded with the parameters $\{s_1, s_2, s_3\}$.
5) The RSUs are secretly preloaded with the parameters $\{SK^{\text{t}}, s_i\}$.

- **Pseudonym and key generation:**
  1) The RSU computes $SK_1^{\text{t}} = s_1 R_t$ and $PK_t = s_t P$. Therefore, the private key of the RSU can be modeled as $(SK_1^{\text{t}}, SK_2^{\text{t}})$.
  2) A vehicle, denoted by $V_i$, chooses a random number $r_i \in Z_q$.
  3) $V_i$ computes $ID_1^i = r_i P$ and $ID_2^i = R ID_i (1) \oplus H(r_i, PK_1)$.
  4) $V_i$ computes $SK_1^i = s_1 ID_1^i$ and $SK_2^i = s_2 H(ID_2^i, ID_2^i)$.

- **Publishing the system parameters:**
  1) The system parameters $(P, q, G_1, G_2, e, PK_1, PK_2, PK_t)$ are preloaded by each VANET member.

The system initialization phase should maintain private materials confidentiality. First, the private master keys $\{s_1, s_2, s_3\}$ are loaded into the vehicle’s tamper-proof device in the system parameters generation process. Any adversary cannot extract any data stored in the device. Second, tamper-proof device is responsible for generating the identity $(ID_1^i, ID_2^i)$ and the corresponding privacy key $(SK_1^i, SK_2^i)$ in the pseudonym and key generation process. Their security is ensured based on the Cyclic Group Discrete Logarithm Problem (CGDLP), so that none can get $s_1$ and $s_2$ from the private key.

The identity information $(ID_1^i, ID_2^i)$ is pseudonym that can achieve privacy preservation, because vehicle $V_i$ will generate a new pseudo identity when entering into the communication range of another RSU, where $ID_1^i = r_i P$, $ID_2^i = R ID_i (1) \oplus H(r_i, PK_1)$, and $r_i$ should be different in different areas. The private keys $(SK_1^i, SK_2^i)$ are used as the verifiers by RSU, which are calculated without $r_i$. Hence, when a vehicle leaves the coverage area of an RSU and enters the coverage area of another RSU, the new RSU can continue to verify their messages with the primary system parameters.

B. Message Signing

The vehicles in a VANET will periodically broadcast messages. To ensure the integrity of messages and the validity of the originators, each messages sent by a vehicle should be signed with its private key. The message signing phase can be modeled as

1) Vehicle $V_i$, where $i \in \{1, 2, 3, \ldots, n\}$, generates a related information $M_i$, where $M_i = M || T$.
2) $V_i$ picks up a pseudo identity $ID_i$ and the corresponding private key $SK_i$ from the tamper-proof device. Then, $V_i$ signs the message $M_i$, where $\sigma_1^i = SK_1^i + h(M_i)SK_2^i$.
3) The tamper-proof device of $V_i$ generates $\sigma_2^i$ with $s_3$, where $\sigma_2^i = (r_i + s_3(h(M_i) + \sigma_1^i))PK_t$.
4) Then, $V_i$ sends the message $\{ID_i, M_i, \sigma_1^i, \sigma_2^i\}$ to the other participants in vicinity.

From the above discussions, one can see that, compared to conventional signatures generated by private keys, we combine $PK_t$ and the private keys of vehicles to sign vehicular messages.

Given a message from a vehicle, the signature attached within the message is shorter than the current standard ECDSA of IEEE1609.2 [9]. With a 160-bit $q$ cyclic group $G^1$, the length of a signature in PBAS is only a half of that of ECDSA, i.e., $|\sigma_1^i| = 21$ bytes. Similarly, $\sigma_2^i$ has the same length, i.e., $|\sigma_2^i| = 21$ bytes. In addition, our signature scheme is an identity-based encryption algorithm, which makes the mapping between identities publicly available. Therefore, the certificate is unnecessary when verifying messages. In other words, only a short-length pseudo identity is sent, i.e., $|ID_i| = |ID_1^i| + |ID_2^i| = 42$ bytes. Conclusively, the signature size of a vehicular message is 84 bytes, i.e., $|ID_i| + |\sigma_1^i| + |\sigma_2^i| = 84$ bytes. Nevertheless, the current standard ECDSA uses 256-byte signature.

C. Batch Verification by Proxy Vehicles

Proxy vehicles can efficiently authenticate multiple messages sent from the other vehicles, then output the result of their authentication process and send it to the entities that have relatively low computing capabilities.

First of all, we propose an efficient proxy vehicle selection strategy. It is crucial to make sure that vehicles have extra computation resources to serve for the others. We consider that $u$ vehicles in the area can communicate with each other directly. Each of them needs to sign and send $a$ messages. We assume that $C_v$ is the cost of authenticating one signature in PBAS, which is undertaken by the proxy vehicles. $C_s$ is the cost of generating one signature. The total computation load of each vehicle $V_i$ is $C_v + ai/C_s$, which is defined as the proxy vehicle selection strategy is explained as follows.

1) When extra resource $C_v + ai/C_s$ satisfies $C_v + ai/C_s > 0$, $V_i$ is qualified to be a candidate of a proxy vehicle.
2) According to $C_v$, denote these extra resources by $(c_1, c_2, \ldots, c_{v,v})$ in a descending order, and the corresponding vehicles by $(p_1, p_2, \ldots, p_{v,v})$, where $0 \leq v_{r,0} \leq u$.
3) Use the median $C_{me}$ of $(c_1, c_2, \ldots, c_{v,v})$ as a threshold, and select the proxy vehicles based on $C_{me} > C_{me}$. The proxy vehicles are defined as $(p_1, p_2, \ldots, p_v)$, where $v$ is the number of proxy vehicles.
4) Each proxy vehicle authenticates the same number of signatures based on the threshold $C_{me}$, which is defined as $(C_{me} - aC_s)/C_s$.

The above selection strategy can be implemented in every vehicles without TA. Based on $(C_v, C_s, C_t)$, vehicles can become proxy vehicles spontaneously to authenticate received signatures. When there are no computation resources in the vehicles, PBAS degenerates to normal authentication schemes. The signature scheme is based on ID-cryptography, and RSUs

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1Every finite cyclic group $G$ is isomorphic to a group $Z_q^+$, where $q$ is the order of the group, and the security of a signature is based on $Z_q^*$.

2We use an MNT curve with 160-bit $q$, which has the same security level with IVB, b-SPECS+, and CPAS.
are not required to pre-store the certificates of proxy vehicles. Hence, there is no upper limitation in the number of proxy vehicles that could be governed by an RSU.

The verification phase in a proxy vehicle can be described as follows.

1) The messages \( \{ID_i, M_i, \sigma^1_i, \sigma^2_i\} \) sent by \( V_i \), \( i \in \{1, 2, 3, \ldots, n\} \), is received by a proxy vehicle \( V_{proxy} \). Then, \( V_{proxy} \) verifies the signatures in batch, i.e., \( \sigma^1_i \), \( i \in \{1, 2, 3, \ldots, n\} \), is valid if the following equation holds.

\[
e \left( \sum_{i=1}^{n} \sigma^1_i, P \right) = e \left( \sum_{i=1}^{n} ID_i^1, PK_k \right) e \left( \sum_{i=1}^{n} h(M_i)H(ID_i^1 \parallel ID_i^2), PK_{K2} \right)
\]

Before the verification process, the proxy vehicle has obtained the public key \((PK_1, PK_2)\), received the message \( M_i \), the signature \( \sigma_i \) of \( M_i \), and the pseudo identity \((ID_i^1, ID_i^2)\) from each surrounding vehicle \( V_i \). Then, \( e \left( \sum_{i=1}^{n} ID_i^1, PK_{K1} \right) e \left( \sum_{i=1}^{n} h(M_i)H(ID_i^1 \parallel ID_i^2), PK_{K2} \right) \) can be calculated by the proxy vehicle, respectively. If these two terms are indeed identical, the integrity of all messages and the identities of senders of these messages are verified. The validity of Eqn. (1) can be verified as follows:

\[
e \left( \sum_{i=1}^{n} \sigma^1_i, P \right) = e \left( \sum_{i=1}^{n} SK_i^1 + h(M_i)SK_i^2, P \right)
\]

\[
e \left( \sum_{i=1}^{n} SK_i^1, P \right) e \left( \sum_{i=1}^{n} h(M_i)SK_i^2, P \right)
\]

\[
e \left( \sum_{i=1}^{n} s_1 ID_i^1, P \right) e \left( \sum_{i=1}^{n} s_2 h(M_i)H(ID_i^1 \parallel ID_i^2), P \right)
\]

\[
e \left( \sum_{i=1}^{n} ID_i^1, s_1 P \right) e \left( \sum_{i=1}^{n} h(M_i)H(ID_i^1 \parallel ID_i^2), s_2 P \right)
\]

\[
e \left( \sum_{i=1}^{n} ID_i^1, PK_k \right) e \left( \sum_{i=1}^{n} h(M_i)H(ID_i^1 \parallel ID_i^2), PK_{K2} \right).
\]

2) Then, \( V_{proxy} \) computes \( \sum_{i=1}^{n} \sigma^1_i \in Z_p^* \), \( \Pi_{i=1}^{n} \sigma^2_i \in Z_p^* \), and sends \( \{M_{proxy}, ID_{proxy}, \sigma^1_{proxy}\} \) to an RSU, where the output denotes \( M_{proxy} = M \parallel \sum_{i=1}^{n} \sigma^1_i \parallel \Pi_{i=1}^{n} \sigma^2_i \parallel T \parallel ID_i, \) \( i \in \{1, 2, 3, \ldots, n\} \), and the verification result is generated by the proxy vehicle and included in \( M \). Here, \( \{M = a\} \) indicates the batch of messages is valid, and \( \{M = b\} \) indicates the batch of messages is invalid. The signature \( \sigma^1_{proxy} \) is generated with \( V_{proxy} \)’s privacy key, \((SK^1_{proxy}, SK^2_{proxy})\).

Given \( n \) distinct messages authenticated by a proxy vehicle, an RSU does not need to receive all the signatures because these signatures have been calculated as \( \sum_{i=1}^{n} \sigma^1_i \) and \( \Pi_{i=1}^{n} \sigma^2_i \). Each proxy vehicle sends the message \( \{M_{proxy}, ID_{proxy}, \sigma^1_{proxy}\} \) to the RSU. The length of the packet is 1264+42n bytes, where \( |ID_{proxy}| = 42 \) bytes, \( |\sigma^1_{proxy}| = 21 \) bytes, and \( |M_{proxy}| = |\sum_{i=1}^{n} \sigma^1_i| + |\Pi_{i=1}^{n} \sigma^2_i| + |h(M_i)| + |ID_i^1 \parallel ID_i^2| \) bytes.

D. Verification by an RSU at Outputs from Proxy Vehicles

RSUs can independently verify the results from the previous verification processes of the proxy vehicles, and then system can exclude false results and revoke malicious proxy vehicles. The verification in an RSU at the outputs from the proxy vehicles includes the following three tasks. Task (1) ensures that the originators of the messages is indeed the real proxy vehicle and there are no forwarding nodes actively modifying messages; Task (2) guarantees that the result from a proxy vehicle contains correct verification output through their batch verification phase; Task (3) revokes the proxy vehicle when RSU finds that it fails the process.

This process can be described as follows.

1) When receiving \( \{M_{proxy}, ID_{proxy}, \sigma^1_{proxy}\} \), the RSU initiates Task (1) to verify if single signature \( \sigma^1_{proxy} \) is valid. The single signature verification process has been proposed and proved in [7]. If it is valid, then TA traces the real identities of this batch of vehicles by computing \( RID_i = ID_i^2 \parallel H(s_i \parallel ID_i^1) \), where \( i \in \{1, 2, 3, \ldots, n\} \).

2) If Task (1) is passed, the RSU goes to Task (2) to check the authentication result sent by a proxy vehicle. The result is valid and the batch of message is authenticated if the following equation holds, or

\[
e \left( \prod_{i=1}^{n} \sigma^2_i, R_T \right) = e \left( \prod_{i=1}^{n} ID_i^1 \left( \sum_{i=1}^{n} h(M_i) + \sigma^1_i \right), SK_{T}^2, SK_{T}^1 \right).
\]

As the RSU has already obtained its private key \((SK^1_{T}, SK^2_{T})\) and extracted \( \sum_{i=1}^{n} \sigma^1_i \), \( \Pi_{i=1}^{n} \sigma^2_i \) from the message \( M_{proxy} \) before, in the verification process the RSU calculates \( e(\prod_{i=1}^{n} \sigma^2_i, R_T) \) with \( R_T \), and
pairing operations.

However, in IBV \[7\], the cost that an RSU spends on verifying signatures is equivalent to that spent on checking a proxy vehicle. The related details of proxy-based authentication scheme are shown in Fig. 3.

3) If Eqn. (3) is not held, the proxy vehicle is considered malicious by RSU. The TA receiving the feedback from the RSU will revoke the malicious proxy, which can prevent it from disturbing the authentication processes later. The algorithm to identify malicious proxy vehicles is showed in Algorithm 1. The security explanation of Steps. 8-13 is given in Section V. A. Security Analysis.

Algorithm 1 The algorithm to identify malicious proxy vehicles.

1. The batch of messages is marked as valid by \(\{M = a\}\), if \(M = a\) || Eqn. (3) is held then 4: if \(M_{proxy}\) is valid then 5: Task (2): verify the result of the proxy vehicle: 6: if \(M = a\) || Eqn. (3) is held then 7: The batch of messages is valid and the proxy vehicle is defined as below.

The validity of Eqn. (3) can be verified as follows:

\[
e \left( \prod_{i=1}^{n} ID_{i} \right) \left( \sum_{i=1}^{n} h(M_{i}) + \sigma_{i}^{2} \right) SK_{i}^{2}, SK_{i}^{2}
\]

Batch key generation process is used when some of vehicles want to establish secrecy links with an RSU. This process can be described as follows.

1) If confidentiality is required, the RSU chooses a random number \(z \in Z_{q}^{*}\) and then computes \(P_{ubr} = zP\) and \(\sigma_{r} = sig_{SK_{r}}(P_{ubr} || T)\). The RSU calculates the session key, i.e., \(K_{r_{i}} = z \cdot ID_{i}^{1}, i \in (1, 2, 3, \ldots, n)\), for each vehicle.

2) The RSU broadcasts a single message, i.e., \(\{P_{ubr}, T, \sigma_{r}\}\). Vehicles that apply for establishing confidentially communications will verify the signature sent by the RSU with \(PK_{r}\), to ensure the validity of the RSU and the integrity of the broadcast messages.

3) Finally, \(V_{i}\) calculates the session key, i.e., \(K_{r_{i}} = r_{i} \cdot P_{ubr}\).

The RSU just needs to generate only one single message to broadcast for a batch of key negotiations. Note that the session keys are distinct because of different vehicles’ contributions on \(r_{i}\). The broadcast message \(\{P_{ubr}, T, \sigma_{r}\}\) by the RSU consists of 21-byte public parameter, 21-byte signature, i.e., \(|P_{ubr}| + |\sigma_{r}| = 42\) bytes. It is noted that the key negotiations and traceability process can be generated offline in a server. Therefore, the key negotiation process will not impose much computational burden on the RSU.

V. SECURITY PERFORMANCE

In this section, we analyze the security and fault-tolerance performance of PBAS. The security analysis of PBAS includes the following four aspects, i.e., message integrity and authentication, replay attack resistance, non-repudiation, and privacy preservation. Particularly, the message integrity and authentication is one of the basic security requirements in VANETs. The fault-tolerance of PBAS is defined as the property that enables the verification process to continue operating properly even in the presence of a small number of compromised proxy vehicles in VANETs. If its operational quality degrades, the degradation is proportional to the number of compromised proxy vehicles, as compared to a naively-designed system, in which even a very small failure can cause the breakdown of an entire system.

A. Security Analysis

1) Message integrity and mutual identity authentication: PBAS achieves mutual identity authentication between RSUs and vehicles. To be authenticated by RSUs, \(V_{i}\) generates signature \(\sigma_{i}^{2}\) of the message \(M_{i}\) with its privacy key \(SK_{i}\). And another signature \(\sigma_{r}^{2}\) is generated by a tamper proof device of \(V_{i}\). Without knowing \(SK_{i}\) and \(s_{3}\), any attacker cannot forge a message and the corresponding signature. Similarly, without knowing RSU’s privacy key \(SK_{r}\), it is computationally infeasible to forge a valid pair \((\sigma_{r}, (P_{ubr}, T))\).

Let us consider a scenario, where the attackers are divided into external and internal attackers. The external attackers are non-authorized entities and can only attain public parameters and public keys. The internal attackers are authorized vehicles.
(such as $V_i$), each of which knows its own privacy key $(SK_i^1, SK_i^2)$ but it cannot extract $s_1, s_2, s_3$ stored in the tamper proof device.

In PBAS, $(SK_i^1, SK_i^2)$ of $V_i$ is changed when the vehicle enters into another coverage area. Without knowing $(SK_i^1, SK_i^2)$, it is impossible to forge a valid signature $\sigma_i = SK_i^1 + h(M_i)SK_i^2$. Due to the CDH problem in $G$, it is infeasible to obtain $s_1$ and $s_2$ from $PK_1$ and $PK_2$. Therefore, any attacker cannot obtain the privacy keys of the others.

If malicious proxy vehicles send bogus results to an RSU, PBAS is secure against these additional attacks as listed in Challenge 1 and Challenge 2.

**Challenge 1**: A proxy vehicle may fool RSUs using the following two possible ways: 1) All messages in a batch are valid but a proxy vehicle claims that there are messages invalid in the batch; 2) There are some messages invalid in a batch, but a proxy vehicle claims that they are all valid.

**Resistance**: In both cases, $\{M_{proxy}, ID_{proxy}, \sigma_{proxy}^1\}$ is still sent to an RSU under the mechanism of PBAS, where the output denotes $M_{proxy} = M \parallel \sum_{i=1}^{n} \sigma_i^1 \parallel T \parallel ID_i$, where $i \in \{1, 2, 3, \ldots, n\}$. It is difficult to forge a valid signature $\sigma_i^1$ and its corresponding $\sigma_i^2$ by cryptographic analysis. In addition, without $s_3$ the attacker is impossible to calculate $\sum_{i=1}^{n} \sigma_i^1$. It is also infeasible to obtain $s_3$ from the formula $\sigma_3^2 = (s_1 + s_3)(h(M_3) + s_1^2)PK_3$, because of the CDH problem in $G$. On the other hand, without $(SK_i^1, SK_i^2)$, a malicious proxy vehicle cannot calculate $\sum_{i=1}^{n} \sigma_i^1$ and $\sum_{i=1}^{n} \sigma_i^2$ from the formula (2) directly, as it is an NP-hard problem. Therefore, PBAS is secure against the attacks of forging bogus results and the corresponding signatures, i.e., $\sum_{i=1}^{n} \sigma_i^1$ and $\sum_{i=1}^{n} \sigma_i^2$. The RSU verifies whether the output of the batch verification by a proxy vehicle is valid with formula (2).

**Challenge 2**: Given the pseudo identity of $V_i$, i.e., $(ID_i^1, ID_i^2)$, and the pseudo identity of $V_j$, i.e., $(ID_j^1, ID_j^2)$, a malicious attacker attempts to confuse the sequence of these authorized vehicles' identities, i.e., $(ID_i^1, ID_i^2)$ and $(ID_j^1, ID_j^2)$, to prevent the TA from tracing the vehicle’s real identity.

**Resistance**: In this case, the formula (2) still holds, but the TA should compute $RID_i = ID_i^2 \oplus H(s_1 \cdot ID_i^1)$, $i \in \{1, 2, 3, \ldots, n\}$, to trace the real identities in the server. The TA will not attain a valid $RID_i$ if the relationship between $ID_i^1$ and $ID_i^2$ is confused.

**2) Replay attack resistance**: In order to guarantee the freshness of messages, $T_R$ denotes the arrival time of a received message, and $T$ denotes the message departure time. $\Delta t_1$ denotes the time difference between vehicle’s clock and local clock, and $\Delta t_2$ denotes the expected network delay. Upon receiving a message, PBAS first checks whether the following inequality is valid, or

$$|T_R - T| < \Delta t_1 + \Delta t_2.$$  

If $T$ is lapsed, then the receivers drop the message. 

**3) Non-repudiation**: Given the pseudo identity $(ID_i^1, ID_i^2)$, only the TA can trace the real identity of a vehicle by $s_1$, or

$$ID_i^2 \oplus H(s_1 \cdot ID_i^1) = RID_i \oplus H(r_i \cdot PK_i) \oplus H(s_1r_i \cdot P) = RID_i.$$ (6)

Finally, the real identity $RID_i$ of a vehicle is obtained. The TA will store $(RID_i, K_r)$ to encrypt the subsequent sensitive messages of services. When a traffic accident occurs, the law enforcement departments can punish the driver of the vehicle.

**4) Privacy preservation**: In PBAS, a vehicle takes advantage of its identity as the public key to reduce the size of signatures, but the disclosure of identity may cause privacy violations. Thus, the real identity $RID_i$ of vehicle $V_i$ is converted into two area-sensitive pseudo identity $(ID_i^1, ID_i^2)$ for privacy protection, where $ID_i^1 = r_i \cdot P$, and $ID_i^2 = RID_i \oplus H(r_i \cdot PK_i)$. Because $V_i$ will regenerate the secret key $r_i$ when entering into a new communication area of another RSU, the pseudo identity and signature, $\sigma_i^1$, $\sigma_i^2$, will dynamically change with the secret key. Without knowing $s_1$, it is impossible to calculate the real identity.

![Fig. 4. Comparison of the authentication schemes (ABAKA and PBAS) in terms of the probabilities for an attacker to successfully trace a vehicle from the pseudo identities of vehicles.](http://www.ieee.org/publications_standards/publications/rights/index.html for more information.)

We use a probability model to analyze the relationship between the probability that an attacker can successfully trace a vehicle and the number of vehicles in the range of an RSU. The successful traceability probability denotes the capability to distinguish one vehicle from the pseudo identities of vehicles in a given period. As shown in Fig. 4, we assume that the number of vehicles is $n$. In ABBKA [10], the attacker should trace a vehicle by selecting the static pseudo identities, where the probability is $P_A(n) = 1/n$. In our scheme, the probability to trace a certain vehicle is $P_P(n) = 1/n^k$, where $k$ is the frequency of changing pseudo identities. If a vehicle passes ten different coverage areas, then we have $k=10$.

**B. Fault Tolerance Analysis**

PBAS takes advantages of the proxy vehicles to realize efficient verification. However, the limitation of the proxy based
verification is that, once a proxy vehicle is compromised, its security performance decreases such that the entire verification process in a batch through the compromised proxy vehicles may lose its efficiency.

The compromised proxy vehicle may come from a variety of ways, such as a loss or misconfigured device, as well as attackers. According to the simulations conducted in Section IV, the average packet loss ratio is generally lower than 0.1%. If a proxy vehicle sends an inaccurate message through a misconfigured device, an RSU can detect it when the verification process fails and then can revoke the vehicle’s certificate. Another situation is that a malicious proxy vehicle forgery or tampers several verification messages in order to pass the batch authentication. This behavior can also be detected with the help of our scheme, as mentioned in Section V. Once a malicious proxy vehicle is detected by RSU, the TA will also revoke the malicious proxy vehicle’s certificate, and this can prevent the malicious proxy vehicle from disturbing the authentication processes later.

Although a compromised vehicle can not obtain any sensitive information, such as others’ secret keys and secret parameters, the server will spend some amount of time on locating the misbehaving nodes, which leads to degrade the performance for our scheme. Considering the above three cases, we assume that at most \( r \) percent of proxy vehicles are compromised and send invalid messages. \( N_v \) denotes the number of vehicles, and \( N_p \) denotes the number of proxy vehicles. Thus, \( N_c = N_p \times r \) denotes the largest number of compromised vehicles in a batch period. We also assume that a proxy vehicle can verify at most \( n \) messages, and each vehicle sends only one message in a batch period. In order to generate an appropriate formula, the number of proxy vehicles that verify more than \( n \) messages is denoted as \( i \). The number of cases that \( N_v \) vehicles are authenticated through \( N_p \) proxy vehicles is equal to

\[
(N_p)^{N_v} - \sum_{i=1}^{[N_v/n]} \left[ \sum_{x=0}^{i-1} (-1)^x \binom{n}{x} \sum_{y=0}^{N_p-n-x} \binom{N_p-N_v-x}{y} \right]. \tag{7}
\]

When \( N_v \gg n \), the eqn. (5) is approaching to \( (N_p)^{N_v} \). Similarly, the number of cases of that vehicles are authenticated through compromised vehicles is equal to \((N_c)^h\). Also, the number of cases that vehicles are authenticated through trusted proxy vehicles is equal to \((N_p-N_c)^{N_v-k}\), where \( k \) denotes the number of vehicles that are authenticated by a compromised proxy vehicle. \( P\{X = k\} \) represents the probability that the verification processes of \( k \) vehicles fail. The probability distribution function conforms to the following formula, or

\[
P\{X = k\} \approx \frac{(N_v)(N_c)^k(N_p-N_c)^{N_v-k}}{(N_p)^{N_v}}. \tag{8}
\]

Fig. 5 shows an example of fault tolerance that there are 100 vehicles in the coverage area of an RSU in a period, the number of proxy vehicles is 20 in this area, and each proxy vehicle can verify 30 messages simultaneously. When the number of compromised vehicles is two, where \( r = 0.1 \), the probability that the verification processes of ten vehicles fail is approximately 0.132. And a backup server must immediately take over these ten failed vehicles. The failure probability of 15 failed vehicles dramatically drops to 0.06. We also observe that there are more failed vehicles as \( r \) increases. Fortunately, the worst probability of this case is much lower. For instance, the probability that the verification processes of 20 vehicles fail is approximately 0.1 when \( r = 0.2 \).

The result shows that PBAS can achieve fault-tolerance and continue its verification operation, possibly with a bit reduced performance, rather than failed completely. With the protection mechanisms of PBAS, RSUs can detect that there are some messages invalid when some compromised proxy vehicles exist. If so, the TA will revoke the compromised proxy vehicle’s certificate. In this way, the number of compromised proxy vehicles is well controlled below 10%\(^3\). They can only make up to 20 failed vehicles, and the failure probability is low enough to be negligible.

VI. PERFORMANCE EVALUATION AND SIMULATIONS

In this section, we evaluate the performance of the proposed PBAS and compare it with the related schemes, such as TESLA++ [5], IBV [6], ABAKA [10], b-SPECS+ [11], and CPAS [12], in terms of computation and transmission overheads. It is noted that TESLA++ uses the standard signature algorithm ECDSA adopted by IEEE 1609.2 [9]. In the simulations, we used ns-2 [39] and a mobility model generation tool called VanetMobiSim [40] to estimate the average messages delays and the average loss ratios of these schemes in a real environment.

A. Computation Overhead Analysis

Here, we evaluate the performance of PBAS and the other schemes in terms of the computation overhead in an RSU.

\(^3\)In [10], it was even believed that the attacker can compromise at most 1% entities subordinated by a TA.
Table II shows the comparison of all schemes for the computation overhead of an RSU in terms of signing a single message and $n$ messages. TESLA++ uses the current standard signature scheme ECDSA, and the total computational time in terms of authenticating $n$ messages is $4nT_{mul}$. Since IBV, CPAS, and b-SPECS+ are used for authenticating safety-related messages, the key negotiation session is excluded in these schemes. To be fair, the computing time in ABAKA spent on key negotiation was not considered.

First, we assume that the traffic density is equal to the number of signatures in a verification period, and each vehicle periodically broadcasts a traffic related message every 300 ms. At least $m$ vehicles should work as the proxy vehicles to verify the messages, and a proxy vehicle can act on at most 300 messages. Thus, $m = \lfloor \frac{n}{300} \rfloor$. In addition, we assume that the communication coverage of an RSU is one square kilometer.

Fig. 6 illustrates the relationship between the number of messages within an RSU’s coverage area and the computation overhead of the RSU. We can see from the figure that the computation overhead increases as the number of messages increases. In addition, we can also see that the computational overhead of TESLA++ is the highest when the number of messages is larger than ten. In other words, the current standard ECDSA scheme is incompatible with the dynamic traffic patterns. PBAS is more efficient when verifying a large number of signatures: when there are more than 40 messages, the computation overhead of PBAS in a RSU is much lower than the others. For instance, in one second, the maximum number of signatures that can be verified by the RSU is approximately 2450, 1000, 1100, and 2000 for CPAS, b-SPECS+, ABAKA, and IBV, respectively. In PBAS, this number reaches 26500.

![Fig. 6](image_url)
three parts, a 42-byte pseudo identity and the other necessary parameters, and each part uses a 160-bit cyclic group (21 bytes), the total signature size of CPAS is 174 bytes. The transmission overhead of CPAS is the largest among these schemes as the number of message increases. While the transmission overhead of ABAKA is smaller because each signature has only a 21-byte parameter and a 42-byte pseudo identity. Also, the total signature size of ABAKA is 63 bytes. The transmission overhead of IBV is the same as ABAKA, i.e., 63 bytes.

Through the aggregation operation, i.e., \((\sigma_1^2 + \sigma_2^2 + \cdots + \sigma_n^2)\) and \((\sigma_1^3 \cdot \sigma_2^3 \cdots \cdot \sigma_n^3)\), in the proxy vehicles, each proxy vehicle sends only a 126-byte packet to RSU to authenticate a batch of messages. The transmission overhead is the smallest if compared with CPAS and ABAKA.

Obviously, the figure shows that the transmission overhead increases linearly with increasing number of messages. The transmission overhead of CPAS is the largest among these schemes, and that of PBAS is much smaller than the others. When the number of messages increases up to 1000, PBAS saves 241 Mbytes and 48 Mbytes of bandwidth compared with CPAS and ABAKA (IBV), respectively. Here, 1000 is the number of messages sent by 300 vehicles in one second.

### C. Simulations

In order to perform a more realistic performance evaluation in simulations, the mobility traces adopted in the simulations were generated using VanetMobiSim [40]. The road scenario of the mobility model for simulations is shown in Fig. 8.

![Road scenario for simulations](image)

**Fig. 8.** Road scenario for simulations. The simulation scenario area length is 8000 meters, which includes four lanes, and each lane is 2000 meters long, four meters wide. The road deploys five RSUs because the transmission range of each vehicle is only 300 meters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Simulation area</td>
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</tr>
<tr>
<td>No. of traffic lane</td>
<td>4</td>
</tr>
<tr>
<td>No. of RSUs</td>
<td>5</td>
</tr>
<tr>
<td>Maximum No. of proxy vehicles</td>
<td>20</td>
</tr>
<tr>
<td>Simulation time</td>
<td>100 s</td>
</tr>
<tr>
<td>MAC protocol</td>
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</tr>
<tr>
<td>Channel bandwidth</td>
<td>6 Mbps</td>
</tr>
<tr>
<td>Transmission range of OBU</td>
<td>300 m</td>
</tr>
<tr>
<td>Transmission range of RSU</td>
<td>1000 m</td>
</tr>
<tr>
<td>Minimum inter-vehicle distance</td>
<td>40 m</td>
</tr>
<tr>
<td>Route protocol</td>
<td>AODV</td>
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<tr>
<td>Slot-time</td>
<td>13 µs</td>
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<tr>
<td>SIFS</td>
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<td>58 µs</td>
</tr>
<tr>
<td>Contention window size (CW)</td>
<td>15~1023</td>
</tr>
</tbody>
</table>

The ns-2.35 [39] was used to simulate the average messages delays and the average loss ratios in RSUs to assess the performance of PBAS. The adopted simulation parameters of DSRC are given in Table IV. The hidden terminal problem is naturally reflected in these two performance parameters in the simulation processes. Especially, the first phase of PBAS is that vehicles broadcast messages in the area. The hidden terminal problem in the broadcast scenario is more severe than that in the second phase of PBAS, in which the proxy vehicles communicate with RSU. To observe and discuss these performance parameters, the average message delay of PBAS is defined as the time to transmit messages from vehicles to an RSU, which can be expressed as

\[
AD_{msg} = \frac{1}{N_T} \sum_{m=1}^{M_{send,m}} \sum_{m=1}^{M_{rsu}} \sum_{p=1}^{t_{trans,m}} \sum_{r=1}^{t_{sign}} \left( T_{msg,m}^{n_{rsu}} + T_{msg,m}^{n_{rsu}} \right)
\]
in which $AD_{msg}$ denotes the average message delay, $V$ denotes the sample area in the simulations, $N_V$ denotes the number of vehicles in $V$, $M_{sent,n}$ denotes the number of messages sent by vehicle $n$, $RSU^n$ is the number of RSUs in the area, and $pro^n$ denotes the number of proxy vehicles. In addition, $T_{sign,n}^m$ denotes the time required for vehicle $n$ to sign message $m$, $T_{trans,n}^m \cdot pro^n$ is the time that vehicle $n$ spends on transmitting message $m$ to the proxy vehicle $n^{pro}$, while $T_{trans,n}^m \cdot RSU^n$ designates the time that the proxy vehicle $n^{pro}$ spends on transmitting message $m$ to RSU, $T_{verify}^{RSU}$ is the time that the proxy vehicle $n^{pro}$ authenticates message $m$, and $T_{verify}^{RSU}$ denotes the time that the RSU checks the result from the proxy vehicle $n^{pro}$.

The average loss ratio is defined as the ratio between the number of messages dropped and the total number of messages received in every 100 second by an RSU, which can be expressed as

$$ALR = \frac{1}{100 \cdot RSU^n} \sum_{n=1}^{RSU^n} \frac{M_{arr}^n}{\sum_{n=1}^{N_V} M_{sent,n}},$$

where $M_{arr}^n$ denotes the number of messages received by RSUs. We run 100 times for each simulation, which lasts 100 s to authenticate messages using the current schemes CPAS, ABAKA, IBV or our proposed scheme PBAS, respectively. For reliability of the simulations, we set 0.95 confidence coefficient as an observed interval.

Fig. 9 shows the first set of simulation results to reveal the relationship between the average message delays and the number of vehicles. In general, the more vehicles appear, the larger the average message delay appears at RSUs. PBAS outperforms ABAKA, IBV, and CPAS, because the proxy vehicles in PBAS reduce the number of handshakes between vehicles and RSUs. From the figure, it is seen that the average message delay of CPAS increases from 50 ms to 110 ms, and that of ABAKA increases from 31 ms to 73 ms when the vehicle density increases from 50 to 100. PBAS performs better than CPAS and ABAKA, whose average message delay increases from 25 ms to 50 ms. From the simulations, we can see that the performance of PBAS is slightly affected by vehicle density.

Fig. 10 shows the second set of simulation results to reveal the relationship between the average message loss ratios in RSUs and the number of vehicles. Vehicles are evenly distributed over different lanes. The speeds of vehicles in each lane are approximately 10~30 m/s.
evaluation model of PBAS showed that PBAS offers fault tolerance, which enables the scheme to continue operating properly even if a small number of proxy vehicles are compromised in VANETs. Moreover, we analyzed and compared the performance of PBAS with the other authentication schemes in terms of their computation and transmission overheads. We also used simulations to verify the efficiency of PBAS in realistic environments, showing that PBAS is a promising security scheme for efficient VANET authentication.

In this work on PBAS, we focused on cryptography algorithm under an assumption that any vehicle having completed system initialization can act as a proxy vehicle. However, it is crucial to make sure that these vehicles have incentives to serve for the others under the condition of efficient message delivery. In the future, we will exploit the game theory to study incentives mechanism. The redundant authentication is another issue, in which different proxy vehicles may work on the same message. To minimize the redundant authentication events, we should design a selection strategy that combines extra computation resource utilization optimization and redundant authentication reduction.

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